

## Chapter 7: Similarity

What I Need to Know	Example
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### 6.1 Properties of Polygons

Classify polygons based on their angles and sides.	<table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <thead> <tr> <th style="padding: 5px;">Number of Sides</th> <th style="padding: 5px;">Name of Polygon</th> </tr> </thead> <tbody> <tr><td style="padding: 5px;">3</td><td style="padding: 5px;">triangle</td></tr> <tr><td style="padding: 5px;">4</td><td style="padding: 5px;">quadrilateral</td></tr> <tr><td style="padding: 5px;">5</td><td style="padding: 5px;">pentagon</td></tr> <tr><td style="padding: 5px;">6</td><td style="padding: 5px;">hexagon</td></tr> <tr><td style="padding: 5px;">7</td><td style="padding: 5px;">heptagon</td></tr> <tr><td style="padding: 5px;">8</td><td style="padding: 5px;">octagon</td></tr> <tr><td style="padding: 5px;">9</td><td style="padding: 5px;">nonagon</td></tr> <tr><td style="padding: 5px;">10</td><td style="padding: 5px;">decagon</td></tr> <tr><td style="padding: 5px;">12</td><td style="padding: 5px;">dodecagon</td></tr> <tr><td style="padding: 5px;">15</td><td style="padding: 5px;">pentadecagon</td></tr> <tr><td style="padding: 5px;">n</td><td style="padding: 5px;">n-gon</td></tr> </tbody> </table>	Number of Sides	Name of Polygon	3	triangle	4	quadrilateral	5	pentagon	6	hexagon	7	heptagon	8	octagon	9	nonagon	10	decagon	12	dodecagon	15	pentadecagon	n	n-gon
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Determine if the polygon is regular, irregular, concave, or convex.																									
Calculate the sum of the interior angles of a polygon. $\ast S_{Int} = (n-2) \cdot 180$	Find the sum of the interior angles of a regular convex 15-gon. $S_I = (15-2)(180)$ $S_I = 2,340$																								
Calculate the sum of the exterior angles of a polygon. $\ast S_E = 360^\circ$	Find the sum of the exterior angles of a regular convex 15-gon. $S_E = 360^\circ$																								

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### 7.1 Ratios in Similar Polygons

Determine if polygons are similar and write a similarity statement.  <u>3 ways to prove <math>\sim \Delta</math>'s</u> AA $\sim$ SAS $\sim$ SSS $\sim$  $\ast \Delta$ 's are $\sim \iff \ast$ sides are proportional	Determine if polygons are similar and write a similarity statement.  <p style="text-align: right;"><math>\Delta</math>'s are <math>\sim</math> by AA or SSS <math>\sim</math></p> <p style="text-align: right;"><b><math>\Delta LMJ \sim \Delta PNS</math></b></p> <p style="text-align: right;">Scale Factor: <math>\frac{5}{2}</math></p> $\frac{45}{18} \stackrel{?}{=} \frac{60}{24} \stackrel{?}{=} \frac{75}{30}$ $2.5 = 2.5 = 2.5 \quad \checkmark$
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**7.2 Ratio and Proportion**

Write and Simplify Ratios and Proportions.  
*cross multiply!*

Solve for x

 ~~$\frac{7}{x+4} = \frac{8}{x}$~~ 

$$7x = 8(x+4)$$

$$7x = 8x + 32$$

$$-x = 32$$

$$x = -32$$

**7.3 Triangle Similarity AA, SSS, SAS**

Identify the postulate used to show triangles are similar.

Determine if the polygons are similar. If so, state the theorem and similarity statement.

$$\frac{3}{18} \stackrel{?}{=} \frac{4}{24} \stackrel{?}{=} \frac{5}{30}$$

$$\frac{1}{6} = \frac{1}{6} = \frac{1}{6} \checkmark$$

yes  $\triangle FDE \sim \triangle CAB$   
 by SSS  $\sim$  *be careful when writing  $\sim$  statement... order matters!*

Find the side lengths of similar triangles.  
*Draw your own Diagram!*  
*match up corresponding sides ... sides are PROPORTIONAL!! (but  $\sim$ )*

$\triangle ABC \sim \triangle XYZ$ . If  $AB = 4$  in.,  $BC = 12$  in.,  $AC = 20$  in., and  $XY = 14$  in., find  $XZ$ .

$$\frac{4}{14} = \frac{20}{x}$$

$$4x = 280$$

$$x = 70$$

$$XZ = 70$$

**7.4 Applying Properties of Similar Triangles**

Use the Triangle Proportionality Theorem to solve for missing segments.

Solve for side LS.

*Option 1: use  $\triangle$  proportionality Thm. (short cut)*

 ~~$\frac{8}{10} = \frac{x}{15}$~~  or  ~~$\frac{8}{x} = \frac{10}{15}$~~ 

$$10x = 120$$

$$x = 12$$

*Option 2: use  $\sim \triangle$ 's (longer...)*

$$\frac{8}{18} = \frac{x}{x+15} \rightarrow 18x = 8(x+15)$$

$$18x = 8x + 120$$

$$10x = 120$$

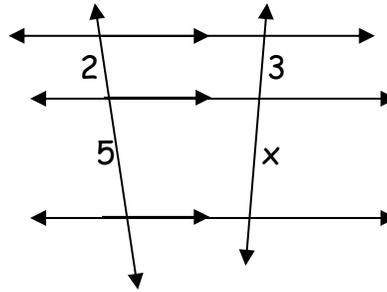
$$x = 12$$

**LS = 12**

Use the Two Transversal Proportionality Corollary to find missing segments.

// lines  $\div$  transversals  
Proportionally!

Find x.



$$\frac{2}{5} = \frac{3}{x}$$

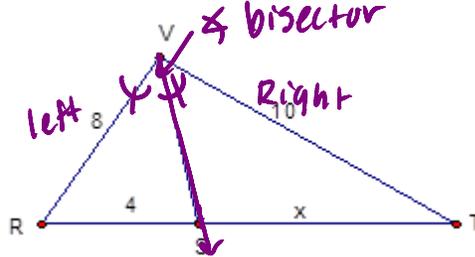
$$2x = 15$$

$$x = 7.5$$

Use the Angle Bisector Theorem to find lengths of segments

$\angle$  bisector  $\div$  sides of  $\Delta$  proportionally!

Given  $\angle RVS \cong \angle SVT$ , find ST



$$\frac{8}{4} = \frac{10}{x}$$

$$8x = 40$$

$$x = 5$$

**ST = 6**

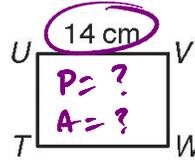
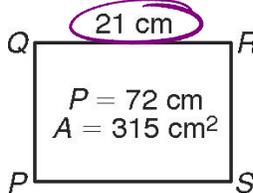
### 7.5 Using Proportional Relationships

Use ratios to make indirect measurements  
Use scale drawings to solve problems.

Ratio of sides = ratio of perimeter

(ratio of sides)<sup>2</sup> = ratio of area

$\square PQRS \sim \square TUVW$ . Find the perimeter and area of  $\square TUVW$ .



Ratio of sides =  $\frac{21}{14} = \frac{3}{2}$

Perimeter

$$\frac{3}{2} = \frac{72}{P}$$

$$3P = 144$$

$$P = 48 \text{ cm}$$

Area

$$\left(\frac{3}{2}\right)^2 = \frac{315}{A}$$

$$\frac{9}{4} = \frac{315}{A}$$

$$9A = 1260$$

$$A = 140 \text{ cm}^2$$

**P = 48 cm**  
**A = 140 cm<sup>2</sup>**

### 7.6 Dilations and similarity in the coordinate plane

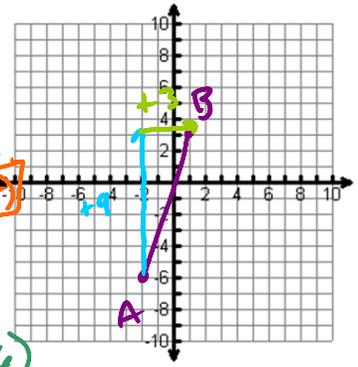
Find points in a coordinate plane that partition a segment proportionally.

Given A(-2, -6) and B(1, 3)

a) Find point P such that P divides the segment from A to B in the ratio 1:5

$$\frac{\text{Rise}}{\text{Run}} = \frac{9 \cdot \frac{1}{6}}{3 \cdot \frac{1}{6}} = \frac{1.5 \uparrow}{.5 \rightarrow}$$

$A(-2, -6)$   
 $+ .5, +1.5$   
**P(-1.5, -4.5)**

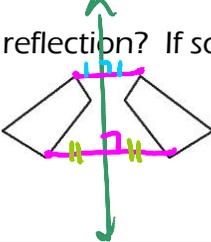


b) Find point Q such that Q divides the segment from A to B in the ratio 2:4

$$\frac{\text{Rise}}{\text{Run}} = \frac{9 \cdot \frac{2}{6}}{3 \cdot \frac{2}{6}} = \frac{3 \uparrow}{1 \rightarrow}$$

$A(-2, -6)$   
 $+ 3, 1$   
**P(1, -5)**

## Chapter 9: Transformations

What I Need to Know	Example
<b>9.1 Reflections</b>	
<p>Identify a Reflection "flip" or "mirror image"</p>	<p>Is it a reflection? If so, draw the line of reflection.</p> <p>yes!</p>   <p>no</p>